

Real-Time Dynamic Modeling: Data Information Requirements and Flight-Test Results

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Practical aspects of identifying dynamic models for aircraft in real time were studied. Topics included the formulation of an equation-error method in the frequency domain to estimate nondimensional stability and control derivatives in real time, data information content for accurate modeling results, speed of convergence, and data information management techniques such as data forgetting, incorporating prior information, and optimized excitation. Real-time dynamic modeling was applied to simulation data and flight-test data from a modified F-15B fighter aircraft and to operational flight data from a subscale jet transport aircraft. Estimated parameter standard errors, prediction cases, and comparisons with results from postflight analysis using the output-error method in the time domain were used to demonstrate the accuracy of the identified real-time models.

Nomenclature

a_x, a_y, a_z	= body-axis translational accelerometer measurements, g or ft/s ²
b	= wingspan, ft
C_X, C_Y, C_Z	= body-axis nondimensional aerodynamic force coefficients
C_l, C_m, C_n	= body-axis nondimensional aerodynamic moment coefficients
\bar{c}	= mean aerodynamic chord, ft
$E\{\}$	= expectation operator
I_x, I_y, I_z, I_{xz}	= mass moments of inertia, slug · ft ²
J	= cost function
j	= imaginary number, $\sqrt{-1}$
M_T	= body-axis pitching moment from engine thrust, ft · lbf
m	= aircraft mass, slug
p, q, r	= body-axis roll, pitch, and yaw rates, rad/s or deg/s
\bar{q}	= dynamic pressure, lbf/ft ²
S	= wing reference area, ft ²
s	= standard error
T	= maneuver length, s
T_x, T_z	= body-axis components of engine thrust, lbf
V	= airspeed, ft/s
α	= angle of attack, rad or deg
β	= sideslip angle, rad or deg
$\delta_c, \delta_{dc}, \delta_s, \delta_{ds}$	= canard, differential canard, stabilator, and differential stabilator deflections, rad or deg
$\delta_e, \delta_a, \delta_r, \delta_f$	= elevator, aileron, rudder, and trailing-edge flap deflections, rad or deg
θ	= parameter vector
Σ	= covariance matrix

φ, θ, ψ	= Euler roll, pitch, and yaw angles, rad or deg
ω	= frequency, rad/s

Superscripts

T	= transpose
\dagger	= complex conjugate transpose
$\hat{}$	= estimate
$\dot{}$	= time derivative
\sim	= Fourier transform
-1	= matrix inverse

Subscript

o	= reference value
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I. Introduction

DYNAMIC modeling in real time has many important practical uses, such as improving the efficiency of stability and control flight testing, flight envelope expansion, adaptive or reconfigurable control, vehicle health monitoring, and fault detection. Several methods [1–5] have been investigated for identifying local linear dynamic models from flight data in real time. One of these methods [4,6] is based on a recursive Fourier transform and equation-error modeling in the frequency domain. This method, sometimes called the Fourier transform regression (FTR) method, produces very accurate results with valid error measures and has many practical advantages. The FTR method has been independently evaluated [7,8] as the best method available for real-time dynamic modeling. For these reasons, the FTR method was chosen for further study and application.

The FTR method has been successfully applied [4,6–11] to identify accurate linear dynamic models in real time at individual flight conditions. Although this capability is important and useful, further progress requires that this capability be extended to continuous application as the aircraft flies through a wide range of changing flight conditions throughout the flight envelope. Ultimately, local real-time modeling results could be integrated into a global aerodynamic model that could be updated in real time as the aircraft changes flight conditions, changes configuration, ages, or becomes damaged in some way. Real-time global dynamic modeling has many important implications for efficient flight testing, accurate flight simulation, adaptive or reconfigurable control, and aircraft safety.

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One important aspect of applying real-time dynamic modeling for varying flight conditions and aircraft configurations is determining the data information content requirements for accurate dynamic modeling results. Changing aircraft flight conditions or aircraft configurations means that parameters in the approximating dynamic model change. Dynamic motion of the aircraft, either from ordinary flight operations or from applied control surface excitation, is necessary so that the aircraft dynamics to be modeled are exhibited in the measured data. Naturally, if the real-time dynamic modeling is to be done continuously or on a regular basis, it is important that only the minimum necessary aircraft excitation be applied, and the resulting aircraft motion should be as small and unobtrusive as possible.

This paper investigates data information requirements for accurate real-time dynamic modeling. Flight experiments on a modified F-15B fighter aircraft are used to illuminate issues related to data information content necessary for accurate real-time modeling. Real-time modeling is also applied to operational flight data from a subscale jet transport aircraft to evaluate the feasibility of real-time modeling without specific excitation. This is an important step in extending local real-time modeling to the case of changing conditions, interpreted broadly to include flight condition changes, configuration changes, damage, and failure scenarios. Issues such as data information content necessary for fast and accurate local modeling, model validation, necessary excitation, data forgetting, and methods for incorporating prior information are studied.

Section II describes the methods used. A model formulation is developed that retains full nonlinear dynamics, with linearized aerodynamic models. The FTR method is described, along with explanations of methods for data forgetting and incorporating prior information into the real-time parameter estimation algorithm. In Sec. III, the flight-test aircraft are described, including the flight instrumentation and characteristics of the flight data. Section IV includes simulation and flight-test investigations examining data information requirements for accurately identifying local dynamic models in real time. Finally, Sec. V summarizes progress made so far and outlines some possible next steps.

II. Methods

A. Aerodynamic Modeling

Nondimensional aerodynamic force and moment coefficients for an aircraft can be computed from flight measurements as follows [6]:

$$C_X = \frac{1}{\bar{q}S} (ma_x - T_x) \quad (1a)$$

$$C_Z = \frac{1}{\bar{q}S} (ma_z - T_z) \quad (1b)$$

$$C_m = \frac{1}{\bar{q}S\bar{c}} [I_y \dot{q} + (I_x - I_z)pr + I_{xz}(p^2 - r^2) - M_T] \quad (1c)$$

$$C_Y = \frac{ma_y}{\bar{q}S} \quad (2a)$$

$$C_l = \frac{1}{\bar{q}Sb} [I_x \dot{p} - I_{xz}(pq + \dot{r}) + (I_z - I_y)qr] \quad (2b)$$

$$C_n = \frac{1}{\bar{q}Sb} [I_z \dot{r} - I_{xz}(\dot{p} - qr) + (I_y - I_x)pq] \quad (2c)$$

These expressions retain the full nonlinear dynamics in the aircraft equations of motion. For local real-time modeling over a short time period, the force and moment coefficients computed from Eqs. (1) and (2) can be modeled using linear expansions in the aircraft states and controls:

$$C_X = C_{X_\alpha} \Delta\alpha + C_{X_q} (\Delta q \bar{c}/2V) + C_{X_\delta} \Delta\delta + C_{X_o} \quad (3a)$$

$$C_Z = C_{Z_\alpha} \Delta\alpha + C_{Z_q} (\Delta q \bar{c}/2V) + C_{Z_\delta} \Delta\delta + C_{Z_o} \quad (3b)$$

$$C_m = C_{m_\alpha} \Delta\alpha + C_{m_q} (\Delta q \bar{c}/2V) + C_{m_\delta} \Delta\delta + C_{m_o} \quad (3c)$$

$$C_Y = C_{Y_\beta} \Delta\beta + C_{Y_p} (\Delta p b/2V) + C_{Y_r} (\Delta r b/2V) + C_{Y_\delta} \Delta\delta + C_{Y_o} \quad (4a)$$

$$C_l = C_{l_\beta} \Delta\beta + C_{l_p} (\Delta p b/2V) + C_{l_r} (\Delta r b/2V) + C_{l_\delta} \Delta\delta + C_{l_o} \quad (4b)$$

$$C_n = C_{n_\beta} \Delta\beta + C_{n_p} (\Delta p b/2V) + C_{n_r} (\Delta r b/2V) + C_{n_\delta} \Delta\delta + C_{n_o} \quad (4c)$$

where Δ indicates perturbation from a reference condition.

In each expansion, a single term is shown to represent all relevant and similar control terms, to simplify the expressions. For example, in Eq. (3c), the term $C_{m_\delta} \Delta\delta$ represents all the control terms for C_m , $C_{m_\delta} \Delta\delta \equiv C_{m_{\delta_e}} \Delta\delta_e + C_{m_{\delta_f}} \Delta\delta_f$. In Eq. (3c), C_{m_o} represents the non-dimensional pitching moment at a reference condition, and similarly for the other expansions.

The linear aerodynamic models in Eqs. (3) and (4) contain parameters called stability and control derivatives, such as C_{m_α} and C_{m_δ} , which characterize the stability and control of the aircraft. For short periods of time, the stability and control derivatives are considered to be constant model parameters to be estimated from flight data. Repeating the parameter estimation at short time intervals produces piecewise constant estimates for the stability and control derivatives, which in general vary with flight condition and changes to the aircraft, such as configuration, age, damage, or failures.

Section II.B describes how the unknown stability and control derivatives in the linear aerodynamic models of Eqs. (3) and (4) can be estimated from flight data using equation-error parameter estimation in the frequency domain.

B. Real-Time Parameter Estimation in the Frequency Domain

This section describes the FTR method for estimating unknown parameters in a dynamic model in real time. Some of the material presented here can also be found in [4,6].

The first step required for modeling in the frequency domain is to transform the measured flight data from the time domain into the frequency domain. The finite Fourier transform is the analytical tool used for this task. For an arbitrary scalar signal $x(t)$ on the time interval $[0, T]$, the finite Fourier transform is defined by

$$\mathcal{F}[x(t)] \equiv \tilde{x}(\omega) \equiv \int_0^T x(t) e^{-j\omega t} dt \quad (5)$$

which can be approximated by

$$\tilde{x}(\omega) \approx \Delta t \sum_{i=0}^{N-1} x(i) e^{-j\omega i \Delta t} \quad (6)$$

where $x(i) \equiv x(i\Delta t)$, $T = (N-1)\Delta t$, and Δt is a constant sampling interval. The summation in Eq. (6) is defined as the discrete Fourier transform,

$$X(\omega) \equiv \sum_{i=0}^{N-1} x(i) e^{-j\omega i \Delta t} \quad (7)$$

so that the finite Fourier transform approximation in Eq. (6) can be written as

$$\tilde{x}(\omega) \approx X(\omega) \Delta t \quad (8)$$

Some fairly straightforward corrections [12] can be made to remove the inaccuracy resulting from the fact that Eq. (8) is a simple Euler approximation to the finite Fourier transform of Eq. (5). However, if the sampling rate is much higher than the frequencies of interest, as is typically the case for dynamic modeling from flight data, then the corrections are small and can be safely ignored.

The Fourier transform is applied to the nondimensional force and moment coefficients computed from Eqs. (1) and (2) using measured time-domain data. This produces the nondimensional force and moment coefficients in the frequency domain. Often, measurements of the angular accelerations \dot{p} , \dot{q} , and \dot{r} are not available. In the frequency domain, these derivatives can be calculated by multiplying the Fourier transforms of p , q , and r by $j\omega$. For example, the Fourier transform of the rolling moment coefficient can be computed as

$$\tilde{C}_l(\omega) \equiv \mathcal{F}[C_l] = j\omega \mathcal{F}\left[\frac{I_x p - I_{xz} r}{\bar{q} S b}\right] + \mathcal{F}\left[\frac{-I_{xz} p q + (I_z - I_y) q r}{\bar{q} S b}\right] \quad (9)$$

and similarly for C_m and C_n . This approach implements the derivative of the body-axis angular momentum in the frequency domain, including the time variation in the inertia quantities. Note that the Fourier transform of the nonlinear terms is handled by computing the nonlinear terms in the time domain, then applying the Fourier transform to the resulting time history. Treatment of the dynamic pressure \bar{q} in Eq. (9) is consistent with an assumption that the dynamic pressure varies slowly, which is a good practical assumption.

To obtain the perturbation states and controls in Eqs. (3) and (4), time histories of the measured states and controls are high-pass filtered to remove the steady part of each signal. Then, each perturbation signal is transformed into the frequency domain using the discrete Fourier transform. The break frequency for the high-pass filter is set just below the lowest frequency selected for the modeling. High-pass filtering is implemented with a fourth-order Butterworth digital filter. Similarly, the quantities transformed in Eq. (9) (shown within the brackets) are high-pass filtered before Fourier transformation. This approach effectively drops out the bias terms in the models of Eqs. (3) and (4), and allows the use of a simple multiplication by $j\omega$ for differentiation in the frequency domain. The high-pass filtering also prevents leakage from the relatively large spectral component at zero frequency (associated with the steady component of each signal) from polluting transformed data at low frequencies.

For each aerodynamic model in Eqs. (3) and (4), the parameter estimation problem can be formulated as a standard least-squares regression problem with complex data [6]:

$$\tilde{z} = \tilde{X}\theta + \tilde{e} \quad (10)$$

where, for example, using the pitching moment Eq. (3c),

$$\tilde{z} = \begin{bmatrix} \tilde{C}_m(1) \\ \tilde{C}_m(2) \\ \vdots \\ \tilde{C}_m(M) \end{bmatrix} \quad (11)$$

$$\tilde{X} = \begin{bmatrix} \Delta\tilde{\alpha}(1) & \Delta\tilde{q}_n(1) & \Delta\tilde{\delta}_e(1) & \Delta\tilde{\delta}_f(1) \\ \Delta\tilde{\alpha}(2) & \Delta\tilde{q}_n(2) & \Delta\tilde{\delta}_e(2) & \Delta\tilde{\delta}_f(2) \\ \vdots & \vdots & \vdots & \vdots \\ \Delta\tilde{\alpha}(M) & \Delta\tilde{q}_n(M) & \Delta\tilde{\delta}_e(M) & \Delta\tilde{\delta}_f(M) \end{bmatrix} \quad (12)$$

$$\theta = \begin{bmatrix} C_{m_\alpha} \\ C_{m_q} \\ C_{m_{\delta_e}} \\ C_{m_{\delta_f}} \end{bmatrix} \quad (13)$$

The notation $\Delta\tilde{q}_n$ represents $\mathcal{F}[\Delta q \bar{c}/(2V)]$, and \tilde{e} represents the complex vector of equation errors in the frequency domain. The symbols $\Delta\tilde{\alpha}(k)$, $k = 1, 2, \dots, M$ denote the Fourier transform of the angle of attack perturbation state for each frequency ω_k and similarly for other quantities. Each transformed variable depends on frequency. The frequencies ω_k can be chosen arbitrarily and are therefore chosen to cover the frequency band in which the aircraft dynamics lie, as will be discussed later. The least-squares cost function is

$$J(\theta) = \frac{1}{2}(\tilde{z} - \tilde{X}\theta)^\dagger(\tilde{z} - \tilde{X}\theta) \quad (14)$$

This cost function contains M squared-error terms in summation, corresponding to M frequencies of interest. Similar cost expressions can be written for individual lines from Eqs. (3) and (4). The parameter vector estimate that minimizes the least-squares cost function is computed from

$$\hat{\theta} = [Re(\tilde{X}^\dagger \tilde{X})]^{-1} Re(\tilde{X}^\dagger \tilde{z}) \quad (15)$$

The estimated parameter covariance matrix is

$$\text{Cov}(\hat{\theta}) \equiv E\{(\hat{\theta} - \theta)(\hat{\theta} - \theta)^T\} = \sigma^2 [Re(\tilde{X}^\dagger \tilde{X})]^{-1} \quad (16)$$

where the equation-error variance σ^2 can be estimated from the residuals,

$$\hat{\sigma}^2 = \frac{1}{(M - n_p)} [(\tilde{z} - \tilde{X}\hat{\theta})^\dagger(\tilde{z} - \tilde{X}\hat{\theta})] \quad (17)$$

and n_p is the number of unknown parameters, which is the number of elements in parameter vector θ . Parameter standard errors are computed as the square root of the diagonal elements of the $\text{Cov}(\hat{\theta})$ matrix from Eq. (16), using $\hat{\sigma}^2$ from Eq. (17). Explanations of why the estimated parameter standard errors are computed in this way, and why this calculation in the frequency domain produces parameter error measures that are consistent with the scatter in parameter estimates from repeated maneuvers, can be found in [6]. Realistic simulation testing has shown that the accuracy of model parameters estimated with this method is comparable to using a time-domain output-error method employing iterative nonlinear optimization in postflight analysis, for which all the data are available [13].

The model formulation given here is widely applicable, because the assumption of constant linear aerodynamic models over short time periods is very accurate for nondimensional stability and control derivatives, where the effects of changing dynamic pressure and mass properties are removed.

To implement this least-squares parameter estimation in the frequency domain, the parameter estimation calculations in Eqs. (15–17) are applied to frequency-domain data at selected times, normally at regular time intervals. The frequency-domain data must therefore be available at any time, and so the Fourier transforms are computed using a recursive Fourier transform, described in Sec. II.C.

C. Recursive Fourier Transform

For a given frequency ω , the discrete Fourier transform in Eq. (7) at time $i\Delta t$, denoted by $X_i(\omega)$, is related to the discrete Fourier transform at time $(i-1)\Delta t$ by

$$X_i(\omega) = X_{i-1}(\omega) + x(i)e^{-j\omega i\Delta t} \quad (18)$$

where

$$e^{-j\omega i\Delta t} = e^{-j\omega\Delta t} e^{-j\omega(i-1)\Delta t} \quad (19)$$

The quantity $e^{-j\omega\Delta t}$ is constant for a given frequency ω and constant sampling interval Δt . It follows that the discrete Fourier transform can be computed for a given frequency at each time step using one addition in Eq. (18) and two multiplications: one in Eq. (19) using the stored constant $e^{-j\omega\Delta t}$ for frequency ω and one in Eq. (18). There is no need to store the time-domain data in memory when computing the discrete Fourier transform in this way, because the data for each sample time is processed immediately. Time-domain data from the past can be used in all subsequent analysis by simply continuing the recursive calculation of the Fourier transform. In this sense, the recursive Fourier transform acts as memory for the information in the data. More data from more maneuvers improve the quality of the data in the frequency domain without increasing memory requirements to store it. Furthermore, the Fourier transform is available at any time $i\Delta t$. The approximation to the finite Fourier transform is completed using Eq. (8).

The recursive computation of the Fourier transform does not use a fast Fourier transform algorithm [14] and, therefore, would be comparatively slow if the entire frequency band up to the Nyquist frequency $1/(2\Delta t)$ were of interest. However, rigid-body dynamics of aircraft lie in a rather narrow frequency band of approximately 0.01–2.0 Hz. Because the frequency band is limited, it is efficient to compute the discrete Fourier transform using Eqs. (18) and (19) [which represents a recursive formulation of Eq. (7)] for only the selected frequencies ω_k , $k = 1, 2, \dots, M$. With this approach, it is possible to select closely spaced fixed frequencies for the Fourier transform and the subsequent modeling and still do the calculations efficiently.

Using a limited frequency band for the Fourier transformation confines the data analysis to the frequency band in which the dynamics lie and automatically filters wideband measurement noise or structural responses outside the frequency band of interest. These automatic filtering features are important for real-time applications, for which instrumentation error corrections and noise filtering would require additional computational resources.

In previous work on fighter aircraft short-period modeling, a frequency spacing of 0.04 Hz on an interval of approximately [0.1–2] Hz was found to be adequate [9–11]. Finer frequency spacing requires slightly more computation, but was found to have little effect on the results. When the frequency spacing is very coarse, there is a danger of omitting important frequency components, and this can lead to inaccurate parameter estimates. In general, a good rule of thumb is to use frequencies evenly spaced at 0.04 Hz over the bandwidth for the dynamic system. For good results, the bandwidth should be limited to the frequency range in which the signal components in the frequency domain are at least twice the amplitude of the wideband noise level. However, the algorithm is robust to these design choices, so that the selections to be made are not difficult.

The recursive Fourier transform update need not be done for every sampled time point. Systematically skipping time points effectively lowers the sampling rate of the data before Fourier transformation. This saves computation and does not have a significant adverse impact on the parameter estimation results until the Fourier transform update rate gets below approximately 5 times the highest frequency of interest for the dynamic system. This lower limit on the update frequency for the recursive Fourier transform is simply to provide sufficient sampling to accurately characterize the frequency content in the measured signals. The parameter estimation and covariance calculations in Eqs. (15–17) can be done at any time, but are usually done at 1 or 2 Hz to save computations. Linearized aerodynamic characteristics rarely change faster than this, except in cases of strong nonlinearity, damage, failure, or rapid maneuvering. For these cases, the update rate can be increased at the cost of more computations.

Estimated parameter standard errors computed from the covariance matrix in the frequency domain using Eq. (16) do not require correction for colored residuals [6]. The standard errors computed from Eq. (16) are therefore a good representation of the error in the estimated parameters. High-quality error measures are important for problems such as failure detection and control law reconfiguration.

D. Data Forgetting

The recursive Fourier transform in Eqs. (18) and (19) represents a data information memory for as long as the running sum is continued. When the aircraft dynamics change, the older data should be discounted in some way, as has been done for time-domain approaches using a forgetting factor [6]. If this is not done, then the speed of response for the real-time parameter estimator is progressively degraded, as new information has to overwhelm an increasingly longer memory. Consequently, there is a tradeoff between the desired rapid response of the parameter estimator to changes in the aircraft dynamics versus retaining enough information from past data for sufficiently accurate model parameter estimates.

If past values of the Fourier transform $X_i(\omega)$ computed from Eq. (18) are saved in computer memory, then it is possible to implement selective amnesia by simply subtracting past values of the running sum corresponding to the Fourier transform or differences

between past values of the running sum. For example, forgetting all data information content older than 10 s (i.e., removing that data information content from the complex regression problem) could be implemented by subtracting the value of the running sums for the Fourier transforms at 10 s ago from the current running sums. Similarly, to forget data information content collected between 5 and 7 s ago, the difference between the running sums at 5 and 7 s ago would be subtracted from the current running sum. The price to pay for this capability is the computer memory required to store past values of the running sums associated with the Fourier transforms for each signal at each frequency. The memory requirements could be reduced by perhaps only saving the running sums at intervals of 0.5 s, for example.

The simplicity of Eq. (18) also makes it easy to see how exponential data forgetting could be implemented. In exponential data forgetting, each past value of the time-domain signal is multiplied by a forgetting factor λ , $0 < \lambda < 1$, at each time step. In this way, old data are gradually devalued and eventually discarded. Usually, λ is chosen in the range of $0.90 \geq \lambda < 1.00$. To implement this, Eq. (18) is modified slightly to

$$X_i(\omega) = \lambda X_{i-1}(\omega) + x(i)e^{-j\omega i \Delta t} \quad (20)$$

and everything else remains the same as before. This simple approach is possible because the Fourier transform is linear with respect to the measured data $x(i)$.

The challenge with data forgetting is not in the implementation, but rather in deciding how much data information content to forget and when. At the present time, there are no concrete guidelines for choosing a value for λ , nor for determining when and how much to forget using selective amnesia. Consequently, these design choices are currently made based on simulation runs and analysis of previous flight data.

E. Incorporating Prior Information

Model parameter estimates can sometimes be improved by including information based on models identified from prior data. In the case of real-time dynamic modeling, including prior information of this kind can reduce variations in the real-time parameter estimates and improve convergence speed.

One way to incorporate prior information is by using a mixed estimator formulation of the least-squares cost function [6]. Assuming that the fit error variance σ_p^2 for the prior modeling is approximately equal to the fit error variance σ^2 for a model based on the current data alone, and denoting the vector of parameter estimates from a prior analysis by θ_p , with associated covariance matrix Σ_p , the least-squares cost function that incorporates this prior information is formulated as [6]

$$J(\theta) = \frac{1}{2}(\tilde{z} - \tilde{X}\theta)^\dagger (\tilde{z} - \tilde{X}\theta) + \frac{1}{2}(\theta - \theta_p)^T \Sigma_p^{-1} (\theta - \theta_p) \quad (21)$$

The vector of parameter estimates that minimize this modified least-squares cost function is

$$\hat{\theta} = [\text{Re}(\tilde{X}^\dagger \tilde{X}) + \Sigma_p^{-1}]^{-1} [\text{Re}(\tilde{X}^\dagger \tilde{z}) + \Sigma_p^{-1} \theta_p] \quad (22)$$

with covariance matrix

$$\text{Cov}(\hat{\theta}) = \sigma^2 [\text{Re}(\tilde{X}^\dagger \tilde{X}) + \Sigma_p^{-1}]^{-1} \quad (23)$$

where σ^2 is estimated from Eq. (17), as before. Further details on the mixed estimator formulation of the least-squares parameter estimation problem and the associated solution can be found in [6].

F. Optimized Excitation

A method for designing optimized inputs for use as control surface perturbations to excite aircraft dynamics is described in [6,11,15]. Each input is a sum of sinusoids with unique frequencies and phase shifts. Multiple inputs are designed to be mutually orthogonal in both

the time domain and the frequency domain and are optimized for maximum data information content in multiple axes over a short time period, while minimizing excursions from the nominal flight condition. The mutual orthogonality of the inputs allows the simultaneous application of multiple inputs, which helps to minimize excitation time. Optimized inputs of this type were applied to the modified F-15B to collect data for real-time dynamic modeling. The optimized inputs were applied as control surface excitations by summation with the actuator commands from the control system just before the actuator command rate and position limiting. Flight-test examples are shown in Sec. IV.

III. Test Aircraft and Flight Data

A. Fighter Aircraft Description

The fighter aircraft used for this research is a preproduction Boeing F-15B that has been highly modified to support various test programs. The most visible modification is the inclusion of a set of canards near the pilot station, seen in Fig. 1. The canards are a set of modified horizontal stabilizers from a Boeing F/A-18 aircraft. The purpose of the canard addition was to increase maneuverability and load capability. An additional effect of the canards was to cause the aircraft to be statically unstable longitudinally at most subsonic speeds. The propulsion system consists of two Pratt & Whitney F100-PW-229 engines, each equipped with an axisymmetric thrust vectoring pitch/yaw balance beam nozzle. The thrust vectoring feature, however, was not used during the flight testing described here. Further information on the modified F-15B aircraft and associated flight-test operations can be found in [16].

1. Control Surfaces

The aircraft has five pairs of control surfaces: stabilators, canards, ailerons, trailing-edge flaps, and rudders. Flaps and aileron droop are manually set by the pilot and only used for takeoff and landing configurations. Conventional pitch control is provided by symmetric deflection of the all-moving horizontal stabilators and canards. Roll control comes from aileron and differential stabilator deflections. Directional control is provided by rudder and differential canard deflections. Definitions of control surface deflections are given below. Trailing-edge down is positive deflection for the wing, canard, and stabilator surfaces, and trailing-edge left is positive for the rudder.

$$\delta_s = \frac{1}{2}(\delta_{s_{\text{right}}} + \delta_{s_{\text{left}}}) \quad \delta_c = \frac{1}{2}(\delta_{c_{\text{right}}} + \delta_{c_{\text{left}}}) \quad (24a)$$

$$\delta_a = \frac{1}{2}(\delta_{a_{\text{right}}} - \delta_{a_{\text{left}}}) \quad \delta_r = \frac{1}{2}(\delta_{r_{\text{right}}} + \delta_{r_{\text{left}}})$$

$$\delta_{dc} = \frac{1}{2}(\delta_{c_{\text{right}}} - \delta_{c_{\text{left}}}) \quad \delta_{ds} = \frac{1}{2}(\delta_{s_{\text{right}}} - \delta_{s_{\text{left}}}) \quad (24b)$$

For the nominal flight control system, pilot stick and rudder pedal inputs result in a high correlation between the symmetric canard and



Fig. 1 Modified F-15B fighter jet aircraft.

Table 1 Geometry and mass properties

	Modified F-15B	S-2
\bar{c} , ft	15.94	0.908
b , ft	42.70	7.083
S , ft ²	608.0	7.046
x_{ref} , in	557.2	42.628
y_{ref} , in	0.000	0.000
z_{ref} , in	116.3	0.000
x_{cg} , in	560.40	42.728
y_{cg} , in	0.14	0.000
z_{cg} , in	117.41	0.519
m , slugs	1234	1.502
I_x , slugs · ft ²	24,830	1.077
I_y , slugs · ft ²	196,225	4.163
I_z , slugs · ft ²	216,155	5.016
I_{xz} , slugs · ft ²	−5329	0.416

angle of attack, rudder and differential canard, and differential stabilator and aileron. Flight data analysis showed that the symmetric canard and angle of attack exhibited a nominal pairwise correlation of 0.93, the rudder and differential canard were correlated at 0.99, and the differential stabilator and aileron were perfectly correlated at 1.00. Given these high levels of correlated inputs, it would be impossible with pilot input maneuvers to distinguish, for example, between a rolling moment generated by the aileron and a rolling moment generated by the differential stabilator. Consequently, the complete stability and control derivative set cannot be obtained with pilot input maneuvers. However, applying the multi-axis orthogonal optimized multisine inputs mentioned earlier results in good data information content, so that all model parameters can be estimated accurately.

2. Instrumentation and Data Acquisition

The modified F-15B aircraft was equipped with a research-quality instrumentation system. A nose boom was installed and calibrated for freestream pitot-static pressure and flow angle measurements. An inertial instrumentation package provided three-axis translational accelerometer and angular rate measurements. Heading, pitch, and bank angle were obtained from the aircraft inertial navigation system. Control surface positions were measured using variable differential transformer sensors. Fuel measurements were obtained from the three fuselage tanks and two wing tanks. Fuel measurements were used to compute the total aircraft weight, c.g., and mass moments of inertia. The mass and geometry characteristics of the aircraft are given in Table 1. The sensor positions and the c.g. location were used to correct the translational accelerometer and flow angle measurements to the c.g. Angular accelerations were not measured. Flight data were collected at 40 Hz.



Fig. 2 S-2 subscale jet transport aircraft.

B. S-2 Subscale Jet Transport Aircraft Description

The S-2 aircraft is a subscale model of a jet transport aircraft. A photograph of the aircraft in flight is shown in Fig. 2. The subscale aircraft has a single jet engine mounted in the aft fuselage and retractable tricycle landing gear. The mass and geometry characteristics of the aircraft are given in Table 1. Further information on the S-2 subscale jet aircraft and associated flight-test operations can be found in [17].

1. Control Surfaces

The control surfaces on the aircraft are a conventional elevator, ailerons, rudder, and inboard trailing-edge flaps. Definitions of control surface deflections are given in Eq. (25). Trailing-edge down is positive deflection for the wing and elevator surfaces, and trailing-edge left is positive for the rudder.

$$\delta_e = \frac{1}{2}(\delta_{e_{\text{right}}} + \delta_{e_{\text{left}}}) \quad \delta_a = \frac{1}{2}(\delta_{a_{\text{right}}} - \delta_{a_{\text{left}}}) \quad (25)$$

The aircraft can be flown by a safety pilot using direct visual contact and conventional radio control. A research pilot executes flight-test maneuvers from inside a mobile control room using a synthetic vision display drawn from telemetry data and a local terrain database. Inputs from the research pilot and ground-based flight

control are used to compute control surface commands, which are transmitted by telemetry to the aircraft.

2. Instrumentation and Data Acquisition

The S-2 aircraft was equipped with a micro-INS, which provided three-axis translational accelerometer measurements, angular rate measurements, estimated attitude angles, and GPS velocity and position. Air data probes on each wing tip (visible in Fig. 2) measured the angle of attack, sideslip angle, static pressure, and dynamic pressure. Measurements from the static pressure sensors and ambient temperature sensors were used to compute air density and altitude. The engine speed in revolutions per minute was measured and used as an input to an engine model to compute thrust. The engine model was identified from ground test data, with adjustments for ram drag identified from flight data [18]. Potentiometers on the rotation axes of the control surfaces measured control surface deflections. Mass properties were computed based on measured fuel flow, preflight weight and balance, and careful inertia measurements of the aircraft on the ground. The pilot stick and rudder pedal commands and throttle position were also measured and recorded. Flight data were collected at 50 Hz.

IV. Results

A. Data Information Requirements for Real-Time Dynamic Modeling

In this section, results will be presented from investigations concerning data information content necessary for accurate real-time modeling.

Figure 3 shows a relationship between the signal-to-noise ratio of aircraft measured responses and the mean error in real-time parameter estimates computed using the FTR method described earlier. Data for this analysis were generated with a linear simulation of the modified F-15B lateral dynamics at a flight condition of Mach 0.75, trim angle of attack of 2 deg, and 20,000 ft altitude. Optimized multisine inputs were applied simultaneously to the lateral control surfaces, as shown in Fig. 4. Repeated simulated data runs with different output signal-to-noise ratios were generated by uniformly reducing the amplitudes of the inputs shown in Fig. 4, generating new simulated outputs, then adding a single realization of noise sequences extracted from flight data to the simulated outputs. This caused the output signal-to-noise ratios to vary in a uniformly decreasing fashion. For each data run, the FTR method was applied, with no prior information, to produce real-time parameter estimates.

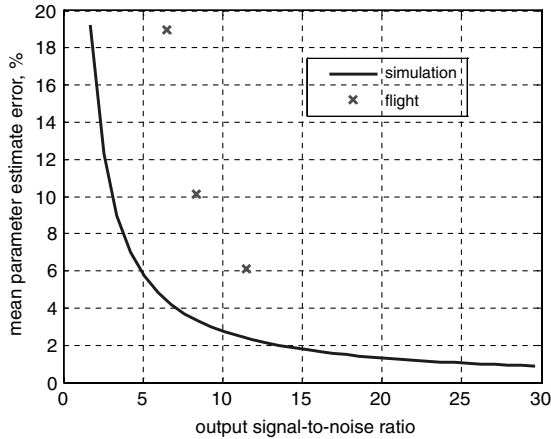


Fig. 3 Dependence of mean real-time parameter estimation error on output signal-to-noise ratio.

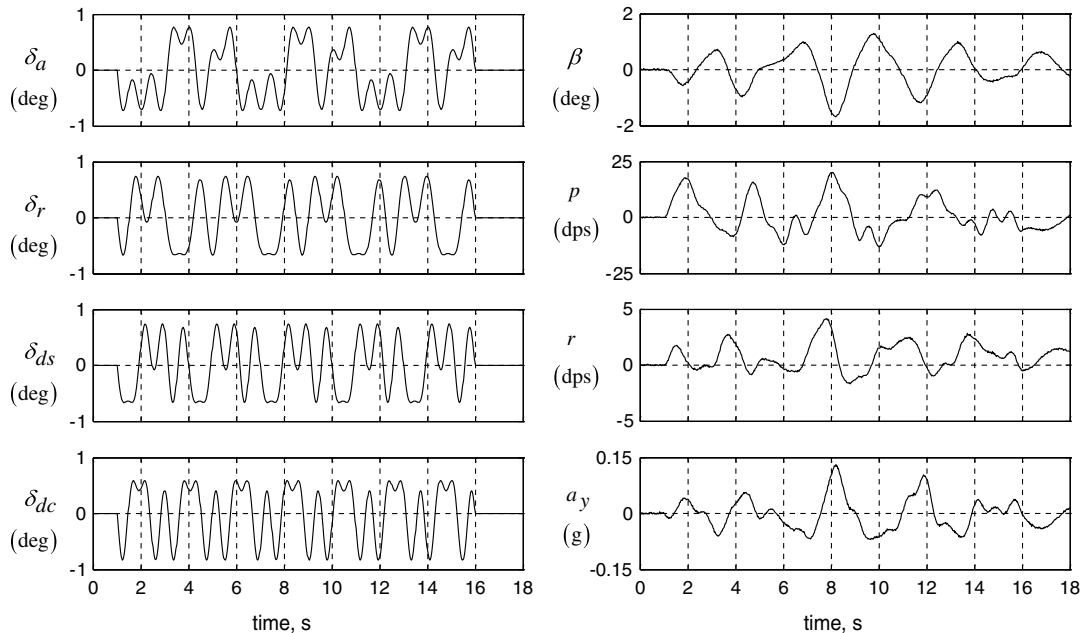


Fig. 4 Simulated data for optimized multisine inputs, modified F-15B aircraft.

Final parameter estimates and standard errors from each 18 s run were used to generate the data points for the solid line in Fig. 3. Because the problem involves multiple parameters and multiple outputs, average values of the parameter estimate errors and output signal-to-noise ratios were used to make the simple summary plot shown in Fig. 3. Based on the solid line in Fig. 3, the signal-to-noise ratios of the measured aircraft responses should preferably be 10 or more, and not less than about 3, for reasonable accuracy of the real-time parameter estimates. This finding is important in designing excitation inputs and also suggests that lower levels of excitation could be used to obtain accurate real-time dynamic modeling if noise levels were decreased. It is of interest to obtain good real-time parameter estimation results with the lowest possible signal-to-noise ratio on the measured outputs, so that the aircraft and pilot are disturbed as little as possible by any excitation applied to the control surfaces. For an output signal-to-noise ratio equal to 10, the input amplitudes were 0.24 deg and the mean parameter estimate error was 2.7%. This choice of input amplitudes produced excellent parameter estimate accuracy, while keeping the rms value of the lateral acceleration a_y below 0.02 g. A typical value for rms lateral acceleration in moderate turbulence is 0.05 g.

Table 2 Pairwise correlation matrix for control surface deflections

	δ_s	δ_c	δ_a	δ_r	δ_{dc}	δ_{ds}
δ_s	1	-0.293	-0.085	-0.026	0.126	0.016
δ_c	—	1	-0.120	-0.065	-0.043	-0.149
δ_a	—	—	1	0.083	0.011	-0.010
δ_r	—	—	—	1	0.177	-0.029
δ_{dc}	—	—	—	—	1	-0.059
δ_{ds}	—	—	—	—	—	1

Similar optimized multisine inputs shown in Fig. 5 were applied to the modified F-15B aircraft in flight at the same flight condition of Mach 0.75, 2 deg trim angle of attack, and 20,000 ft altitude. The aircraft is longitudinally unstable at this flight condition, which means that feedback control was operating when the control surface excitations were applied by summation with actuator commands from the control system. As shown in Fig. 5, all longitudinal and lateral control surfaces were moved simultaneously. The dashed lines show the optimized multisine input design, for which the inputs are mutually orthogonal in both the time and frequency domains.

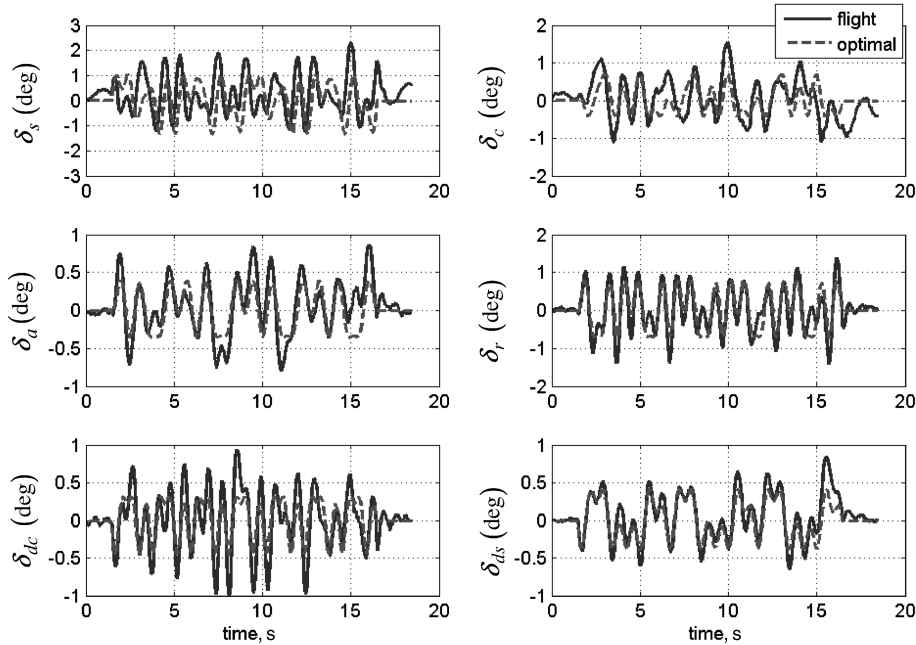


Fig. 5 Optimized multisine input distortion, modified F-15B aircraft.

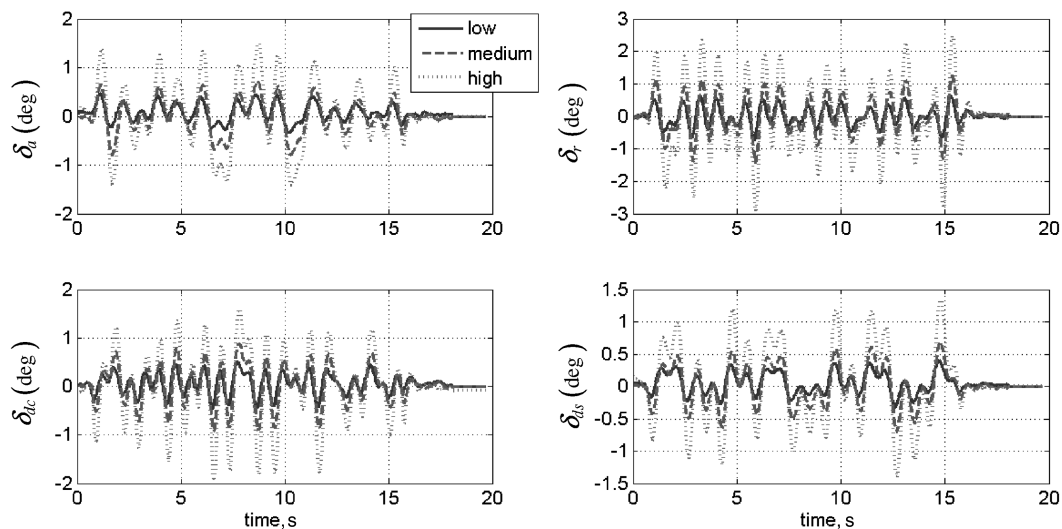


Fig. 6 Input amplitude variation, modified F-15B aircraft.

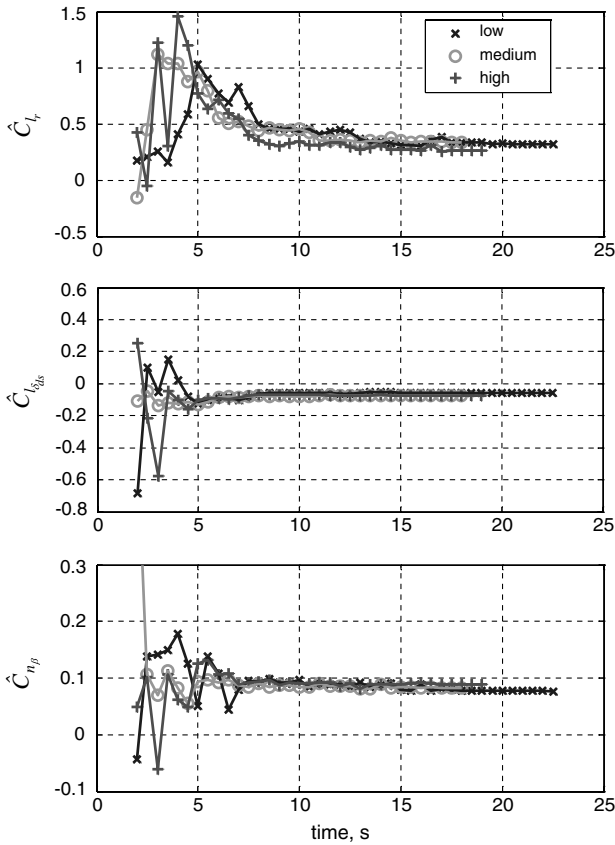


Fig. 7 Real-time parameter estimates for varying input amplitudes, modified F-15B aircraft.

The solid lines show the actual control surface measurements in flight, which are distorted from the optimal waveforms by the feedback control. The highest pairwise correlation for control surface deflections is between stabilator δ_s and canard δ_c , because of the high-gain feedback necessary to compensate for the longitudinal instability at this flight condition. Nevertheless, the control surface deflections were largely uncorrelated, as shown by the pairwise correlation coefficients listed in Table 2. These correlation levels are well below the 0.9 correlation level typically used as an upper limit for allowable correlation of explanatory variables [6]. Although the relatively high-gain feedback control ruined the input orthogonality, the data still exhibited very low correlations among the control surface deflections, which is desirable for accurate dynamic modeling [6].

Using optimized multisine inputs, the effect of input amplitude was investigated in flight by repeating maneuvers with varying input amplitudes. Figure 6 shows the variation in amplitudes for lateral control surface deflections. Selected real-time parameter estimates are shown in Fig. 7. The markers indicate real-time parameter

estimates, and the lines only connect these markers to more clearly show the evolution of the parameter estimates. Real-time modeling was done using the FTR method with no prior information, a frequency vector $f = [0.10 \ 0.12 \ \dots \ 2.00]$ Hz, recursive Fourier transform run at a data rate of 40 Hz, and real-time parameter estimation calculations done at 2 Hz. Selections for the frequency vector and update rates were not critical to the results produced; similar results could be obtained for a fairly wide range of choices of these quantities. The results shown in Fig. 7 are typical examples of the real-time parameter estimation results. The excitation amplitudes made little difference in either the speed of convergence or the final parameter estimates. In general, control derivative estimates (e.g., $\hat{C}_{l_{b_{ds}}}$) were the fastest to converge and usually the most accurate, followed by static stability derivative estimates (e.g., $\hat{C}_{n_{\beta}}$) and damping parameter estimates (e.g., \hat{C}_{l_r}). Roughly 8 s of excitation was required for all model parameters to converge, with no prior information. Standard errors are not shown in Fig. 7 to reduce clutter on the plots.

The mean signal-to-noise ratios for the measured lateral aircraft responses in flight to low-, medium-, and high-amplitude inputs were 6.5, 8.4, and 11.5, respectively, with mean parameter estimate errors of 19.0, 10.1, and 6.1%, respectively. These results are shown by the x markers in Fig. 3 and exhibit the same character as the simulation results shown in Fig. 3, but with higher mean parameter errors. This is expected, because flight data have noise components from structural responses, nonlinearities, and model structure errors that are not present in the linear simulation. This results in higher mean parameter errors for flight data analysis and modeling. The rms values of the lateral acceleration a_y for low-, medium-, and high-amplitude inputs were 0.012, 0.024, and 0.045 g, respectively, compared to 0.05 g, which is typical for moderate turbulence.

Variation in the frequency content of the excitation inputs was studied by applying two different optimized excitation input designs in flight, one for a short (6 s) time length and consequently more sparse frequency content, and one with a longer (15 s) time length and richer frequency content. A comparison of the frequency content for the two optimized input designs is shown in Fig. 8 for the longitudinal controls only. The spectra comparison for lateral controls was similar. Both optimized input designs were flown on the modified F-15B aircraft at the same flight condition as before. Typical real-time parameter estimation results are shown in Fig. 9, with 95% confidence intervals, based on estimated parameter standard errors, shown by the vertical bars through each estimate. In general, the more sparse frequency content led to slightly poorer convergence and accuracy, except for control derivatives like $\hat{C}_{n_{\beta}}$. Figure 9 shows that a more effective approach for short excitation times is to truncate a maneuver designed for a longer time length, because the longer maneuver has a wider variety of frequencies, more closely spaced along the frequency axis, cf. Fig. 8.

Figure 10 shows a comparison of selected real-time parameter estimates based on flight data from the modified F-15B aircraft at the same flight condition. Optimized multisine excitation was done first by moving only the longitudinal control surfaces (δ_s and δ_c)

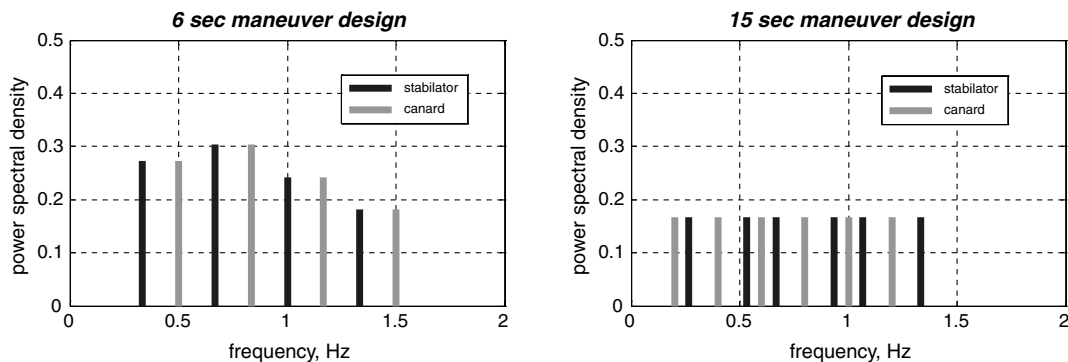


Fig. 8 Excitation input spectra for 6 and 15 s longitudinal controls, modified F-15B aircraft.

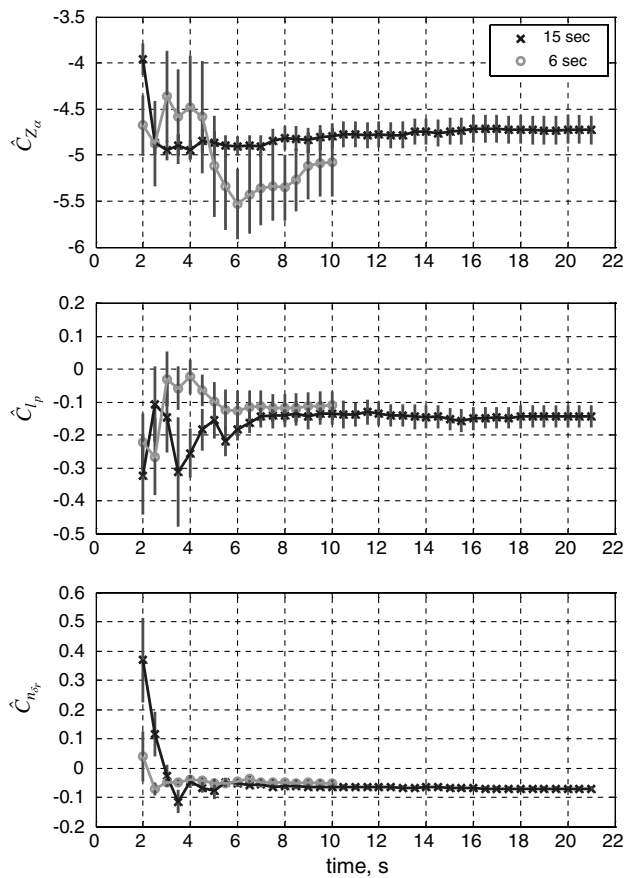


Fig. 9 Real-time parameter estimates for varying frequency content, modified F-15B aircraft.

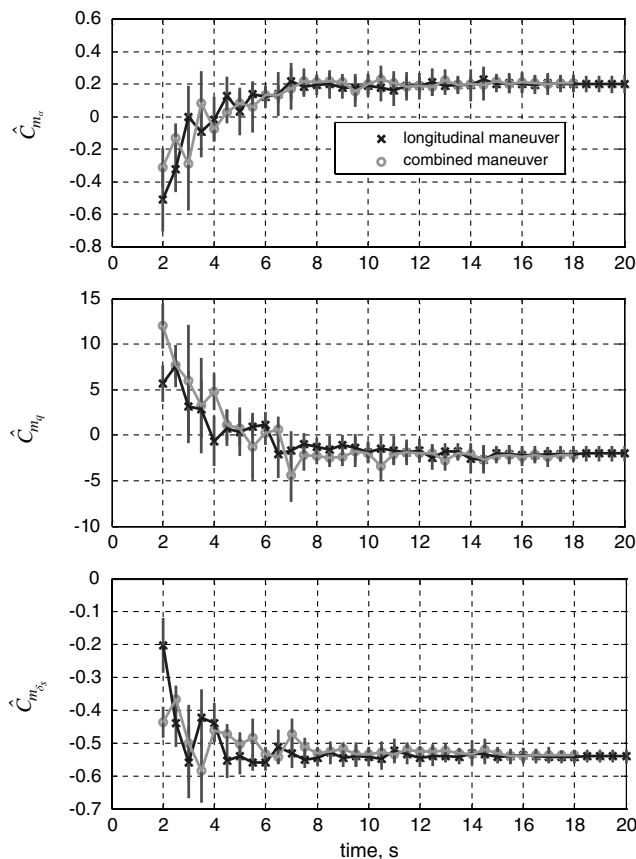


Fig. 10 Real-time parameter estimates for combined maneuver compared with longitudinal only, modified F-15B aircraft.

simultaneously, then again moving all longitudinal and lateral control surfaces (δ_s , δ_c , δ_a , δ_r , δ_{dc} , and δ_{ds}) simultaneously. The results in Fig. 10 show that there was essentially no difference in the real-time parameter estimation behavior for these cases, indicating that the multiple input design was effective, that the equation-error parameter estimation worked as expected on each equation individually, and finally that there was negligible aerodynamic coupling for the maneuvers resulting from these optimized excitation inputs. Similar results were found when comparing lateral excitation alone to combined longitudinal and lateral excitation. Real-time parameter estimate behavior for other model parameters was similar to that shown in Fig. 10 for the three selected longitudinal parameters.

The results in Fig. 10 indicate that combined longitudinal and lateral maneuvers with all control surfaces moving at once should be used for maximum efficiency in real-time dynamic modeling. This approach can provide a full set of stability and control modeling results in a single relatively short maneuver. Finally, Fig. 10 shows that the FTR method has no trouble identifying dynamic model parameters when the aircraft is statically unstable longitudinally ($C_{m_{\alpha}} > 0$), as in this case.

B. Prior Information

The real-time dynamic modeling results shown in Figs. 7, 9, and 10 were generated with the FTR algorithm assuming no prior information. If, instead, the FTR algorithm is provided some information about the values of the model parameters, in terms of parameter estimates and an associated covariance matrix from a previous analysis, the convergence behavior of the real-time parameter estimates from the FTR method changes. Figure 11 shows real-time parameter estimate histories for a combined longitudinal and lateral maneuver using medium-amplitude optimized multisine excitation and no prior information, along with real-time parameter estimate histories using the same data, but with prior information from parameter estimates and an associated covariance matrix at the end of a low-amplitude

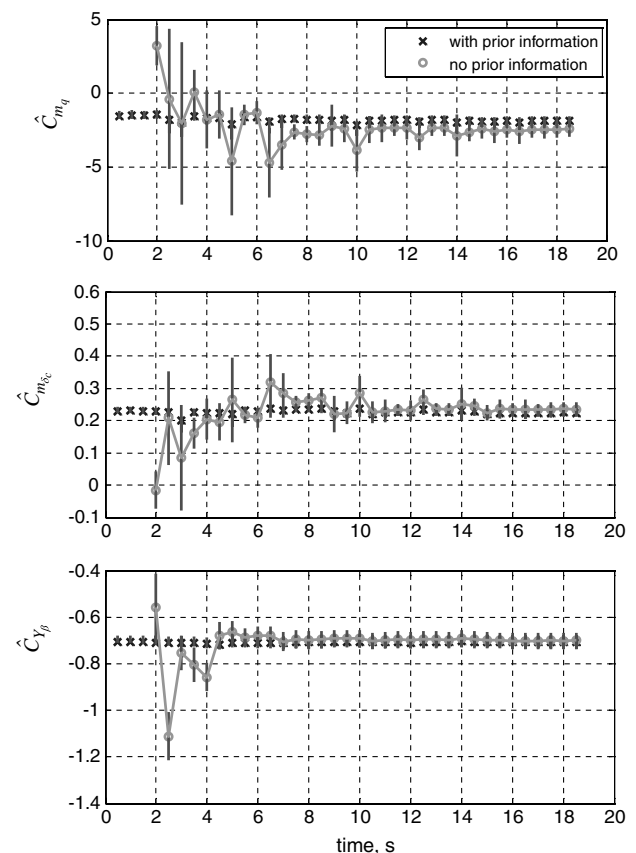


Fig. 11 Real-time parameter estimates with and without prior information, modified F-15B aircraft.

Table 3 Converged real-time parameter estimates for the modified F-15B from combined longitudinal/lateral optimized multisine flight-test maneuvers, where $V_o = 793$ ft/s, $h_o = 20,000$ ft, and $\alpha_o = \theta_o = 2$ deg

Parameter θ	Estimate $\hat{\theta}$	s
C_{Z_a}	-4.5302	0.0397
C_{Z_q}	-12.6864	0.6370
$C_{Z_{\delta_s}}$	-0.4958	0.0150
$C_{Z_{\delta_c}}$	-0.1816	0.0238
C_{m_a}	0.2339	0.0234
C_{m_q}	-2.9742	0.3746
$C_{m_{\delta_s}}$	-0.5521	0.0088
$C_{m_{\delta_c}}$	0.2544	0.0140
C_{Y_β}	-0.7646	0.0114
C_{Y_r}	1.7568	0.1402
$C_{Y_{\delta_a}}$	0.0264	0.0064
$C_{Y_{\delta_r}}$	0.2068	0.0038
$C_{Y_{\delta_{dc}}}$	-0.0980	0.0057
$C_{Y_{\delta_{ds}}}$	0.1546	0.0068
C_{l_β}	-0.0678	0.0037
C_{l_p}	-0.2009	0.0104
C_{l_r}	0.2383	0.0432
$C_{l_{\delta_a}}$	-0.0625	0.0020
$C_{l_{\delta_r}}$	0.0048	0.0012
$C_{l_{\delta_{dc}}}$	0.0005	0.0018
$C_{l_{\delta_{ds}}}$	-0.0777	0.0024
C_{n_β}	0.0945	0.0041
C_{n_p}	-0.0348	0.0115
C_{n_r}	-0.3154	0.0477
$C_{n_{\delta_a}}$	-0.0092	0.0023
$C_{n_{\delta_r}}$	-0.0805	0.0013
$C_{n_{\delta_{dc}}}$	-0.0518	0.0020
$C_{n_{\delta_{ds}}}$	-0.0474	0.0027

combined maneuver. Real-time estimate variations are greatly reduced with the addition of prior information, particularly at the beginning of the maneuver. However, this regularization also results in something like a weighted average for the final parameter estimate, which is different from what would be computed with no prior

information, as can be seen in the top plot of Fig. 11 for \hat{C}_{m_q} . The extent of this effect depends on the values and accuracy of the parameter estimates provided as prior information.

C. Model Validity

The quality of the estimated parameter error bounds can be judged by how well those error bounds characterize the difference between the associated real-time parameter estimate and the final converged parameter estimate. The computed error bounds from the FTR method accurately characterized these differences, which is consistent with similar findings in previous work [6,13]. Although such a measure is easy to compute postflight (when the converged values are known), metrics that can be computed in real time must be devised. The adequacy of local real-time dynamic models can be assessed using short-term prediction tests or tests involving the size of the estimated parameter standard errors. Various metrics have been proposed, but research continues toward devising a generally applicable metric for real-time model validation.

Table 3 gives parameter estimates and standard errors from the FTR method at the end of a high-amplitude lateral maneuver (for the lateral parameters) and a medium-amplitude longitudinal maneuver (for the longitudinal parameters) with no prior information. Separate maneuvers with different amplitudes were chosen to more closely match the amplitudes of doublet maneuvers used for prediction testing. The model parameters given in Table 3 were used with control surface deflections from pilot doublet maneuvers to check the prediction capability of the identified models. Bias terms for the aerodynamic models were estimated in the time domain [6], because the frequency-domain modeling excludes the biases.

Figures 12a and 12b shows model predictions using flight data from a longitudinal pilot doublet maneuver and a lateral/directional pilot doublet maneuver, respectively. For these pilot doublet maneuvers, the control surface deflections were highly correlated with one other and with aircraft responses. Consequently, pilot doublet maneuvers could only be used for prediction cases, and not for model identification. In Fig. 12, the responses predicted with models identified from multisine inputs match the flight data within the noise level of the measured responses of the aircraft for most of each maneuver. The prediction capability shown in Fig. 12 is excellent for these doublet maneuvers, which have very different input forms than the multisine inputs used in the identification maneuvers. This gives high confidence in the validity of the identified models.

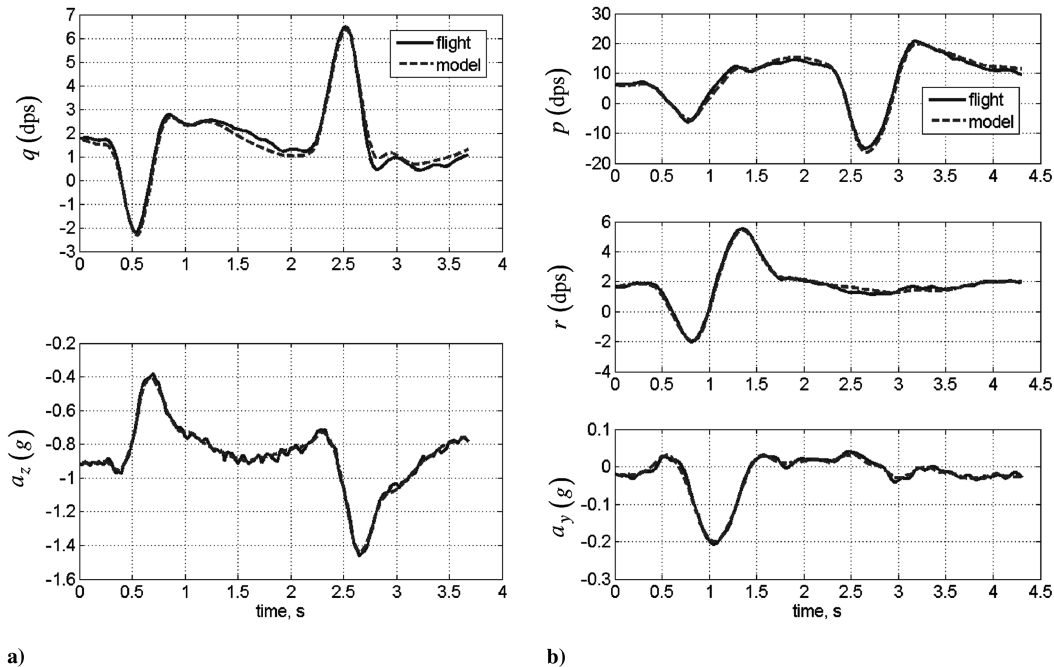


Fig. 12 Prediction cases using real-time parameter estimates, modified F-15B aircraft.

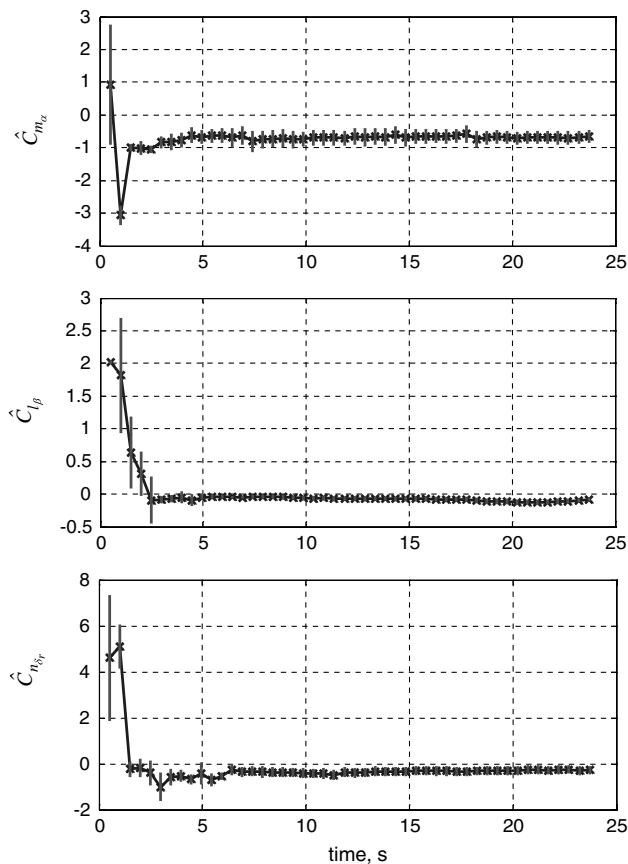


Fig. 13 Real-time parameter estimates during approach in landing configuration, S-2 aircraft.

D. Real-Time Dynamic Modeling in Operational Flight

All of the flight testing for dynamic modeling on the modified F-15B aircraft was at a single flight condition using various optimized excitation inputs. To investigate the performance of the real-time dynamic modeling method in operational flight with low data information content, flight data from the S-2 subscale jet transport aircraft in normal approach (i.e., without specific excitation inputs) were used. Figure 13 shows real-time parameter estimation results for the S-2 aircraft during approach in landing configuration (full flaps, landing gear down). The real-time parameter estimates shown in Fig. 13 were obtained with no prior information.

The real-time dynamic modeling results in this case are of similar quality to the results obtained with optimized multisine excitation inputs. Part of the reason for this is that the S-2 aircraft must be actively controlled by the pilot during approach to landing, and there is no feedback control system operating. However, these results show encouraging success in estimating real-time dynamic model parameters without specific control surface excitation. Further flight data have been collected with the S-2 aircraft, which has been equipped with the capability to apply arbitrary excitations to any or all control surfaces. These data will be used to investigate lower limits on signal-to-noise ratios for real-time dynamic modeling in changing flight conditions and for real-time dynamic modeling near stall and departure.

Real-time dynamic modeling was also applied in S-2 flight testing during three-axis pilot doublet maneuvers (pitch, yaw, and roll doublets, in sequence), with results displayed inside the mobile operations station (MOS) [18] in real time. Figure 14 shows the real-time display for selected parameter estimates during a three-axis pilot doublet maneuver at 80 kt and 800 ft altitude. The dashed lines (added postflight) indicate values of the parameter estimates obtained with a time-domain output-error method that employs an iterative nonlinear optimizer for postflight data analysis and modeling using all of the data from the maneuver [6]. It is evident that, after only a few seconds of data, the real-time dynamic modeling algorithm (operating with no prior information) computed very accurate stability and control derivative estimates. Note that each stability or control derivative is inaccurate until the relevant measured quantity shows some significant variation (i.e., data information content), after which the associated derivative estimate converges quickly. Finally, the 95% confidence intervals for the parameter estimates, indicated by the vertical bars through each parameter estimate marker, properly characterize the accuracy of the real-time parameter estimates.

V. Conclusions

Simulation and flight testing were used to investigate data information requirements for accurate real-time dynamic modeling from noisy data. Applying real-time parameter estimation in the frequency domain with optimized multi-axis multisine excitation inputs was shown to be an effective and accurate method for real-time dynamic modeling. With proper data information management, this approach could be applied to changing flight conditions that occur throughout a flight and could be used to characterize aircraft dynamics in cases of failure or damage.

A real-time dynamic modeling algorithm was described in detail. The algorithm uses equation error in the frequency domain, full nonlinear equations of motion with linearized nondimensional

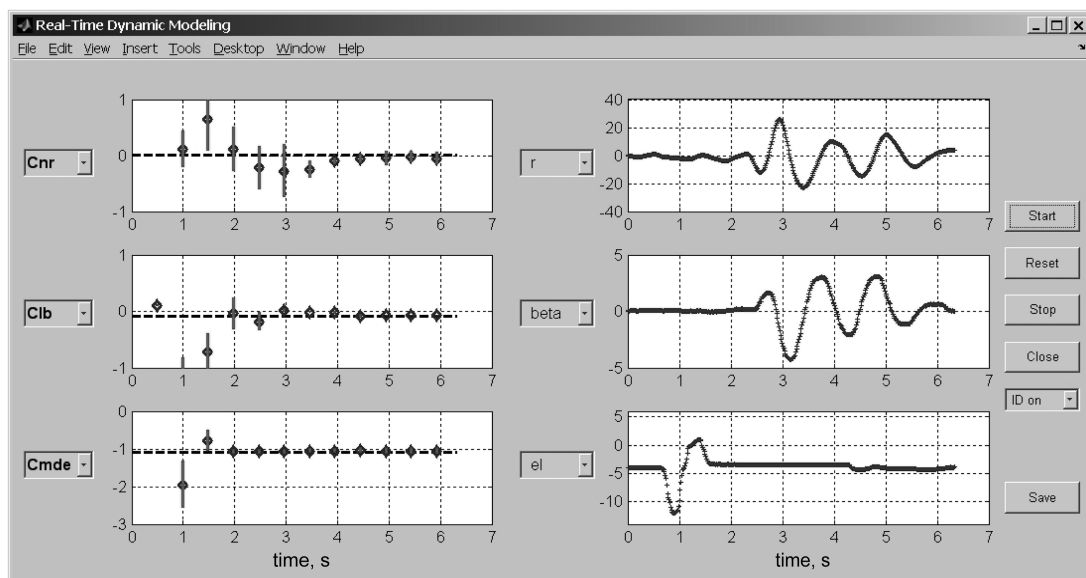


Fig. 14 Real-time parameter estimates for a three-axis pilot doublet maneuver, S-2 aircraft.

aerodynamics, least-squares regression with complex numbers, and a recursive Fourier transform. Modifications necessary to incorporate information from a previous analysis into the least-squares formulation, or to implement data forgetting in the frequency domain in the form of selective amnesia or a multiplicative forgetting factor, were developed and explained.

Results from flight investigations on a modified F-15B aircraft showed that using real-time parameter estimation in the frequency domain, combined with optimized multisine inputs, provided accurate real-time dynamic modeling results, even for noisy flight data from an open-loop unstable aircraft operating with high-gain feedback control. Mean signal-to-noise ratios of aircraft flight responses were shown to be nonlinearly and inversely correlated with mean real-time parameter estimation error, based on analysis of both simulation data and flight data from the modified F-15B aircraft. This provides important design guidance for the excitation and suggests that smaller excitations can be used as the measurement noise levels get smaller, making the required excitations less noticeable to the pilot and passengers.

Refinements to the optimized excitation input designs were identified based on flight results. Increased input amplitudes were found to have little effect on model parameter accuracy or convergence. Richer frequency content in the excitation inputs produced more accurate estimates of stability derivatives in a shorter time. Consequently, truncating inputs designed for longer periods of excitation was found to be a superior approach, compared to using inputs designed specifically for shorter excitation periods. Combined longitudinal and lateral optimal excitations were found to be just as effective as separate longitudinal or lateral optimized inputs. This means that multi-axis optimized inputs can be used to efficiently provide data information content for real-time dynamic modeling in all axes simultaneously, which reduces the time required.

Incorporating information about the dynamic model parameters from a prior analysis into the real-time modeling algorithm significantly reduced variability in real-time parameter estimates, particularly at the start of a maneuver. However, using this approach made the parameter estimator respond more slowly to changing aircraft stability and control characteristics, and can introduce biases in the parameter estimates when the prior information applies to a different flight condition or aircraft configuration.

Real-time estimates of parameter errors computed from flight data were found to properly characterize the accuracy of the real-time parameter estimates, even in initial transient periods. This feature is critically important for many practical applications, such as fault detection and adaptive or reconfigurable control. Dynamic models identified in real time agreed closely with postflight analysis results and exhibited excellent prediction capability for maneuvers with dissimilar input forms. Flight data from a subscale jet transport aircraft were used to show that the real-time dynamic modeling also works well for three-axis pilot doublet maneuvers, as well as during ordinary flight operations, such as approach to landing.

Additional work is necessary on the data information management problem, for example, determining how much data information to forget and when, and deciding when control surface excitations should be applied. The contributions of this paper include how to specify and implement effective yet minimal excitation for real-time dynamic modeling, how to formulate and solve the real-time dynamic modeling problem in a practical setting, and how to implement data information management techniques such as incorporating prior information and data forgetting in the frequency domain, along with flight-test demonstrations of the effectiveness of these ideas. Adding a solution to the data information management problem would result in a comprehensive real-time identification scheme applicable to changing flight conditions and different aircraft configurations, including aircraft degradations such as aging, damage, and failures.

Uses for real-time dynamic modeling results include improving the efficiency of stability and control flight testing, adaptive or reconfigurable control, and providing real-time stability and control information to the pilot for improved flight safety. Local linear models identified in real time can be also used to track eigenvalues

and eigenvectors of the dynamic system. This information could be used in bifurcation analysis for nonlinear flight regimes to characterize and predict departure from controlled flight.

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